Addition and Subtraction Strategies for Single-Digit Numbers			
(see p. 31 <i>in Children's Mathematics</i> ) (see chapter 3 <i>in Children's Mathematics</i> for narrative description)			
Direct	<ul> <li>represents all quantities</li> <li>follows action or situation</li> </ul>		
Modeling	of the story		
Counting	<ul> <li>conserves one number in his/her head</li> <li>counts on or back by ONES</li> </ul>		
Derived	• uses an add. /sub. fact they		
Facts and/or	know to solve one they don't know (derived fact)		
Recalled	• knows add. /sub. fact from		
Facts	memory (recalled fact)		
Flexible	strategy does not match action or situation of the problem		
Strategies			
(this can be evident in any of the above three stages)			

## Addition and Subtraction Strategies for Multi-Digit Numbers

(see p. 74 in Children's Mathematics) (see chapter 6 in Children's Mathematics for narrative description)

for narrative description)		
Direct Modeling by 1's	<ul> <li>represents each quantity as a collection of single units</li> <li>follows action or situation of the story</li> </ul>	
Direct Modeling by 10's	• represents each quantity, uses at least some groups of tens to represent quantities	
Counting	<ul> <li>conserves one number in his/her head</li> <li>counts on or back by ONES</li> </ul>	
Invented Algorithms (see pages 70-74 for more detailed information in Children's Mathematics)	<ul> <li>Incrementing strategy</li> <li>Combining like units strategy</li> <li>Compensating Strategy</li> </ul>	
Flexible Strategies (this can be evident in any of the above four stages)	strategy does not match action or situation of the problem	

## Multiplication and Division Strategies for Single-Digit Numbers

(see pages 34-44 in Children's Mathematics) (see chapter 4 in Children's Mathematics for narrative description)

	•
Direct Modeling	<ul> <li>represents all quantities</li> <li>follows action or situation of the story</li> </ul>
Counting	<ul> <li>SKIP counts</li> <li>repeated addition/ subtraction</li> </ul>
Derived Facts <sup>and/or</sup> Recalled Facts	<ul> <li>uses a mult. or division fact they know to solve one they don't know (derived fact)</li> <li>knows mult. or division fact from memory (recalled fact)</li> </ul>
Flexible Strategies (this can be evident in any of the above three stages)	strategy does not match action or situation of the problem

## Multiplication and Division Strategies for problems with Groups of 10 or 100

(see p. 64 in Children's Mathematics ) (see chapter 6 in Children's Mathematics for narrative description)

Counting by 1's	• counts every unit by ones
Counting by 10's	• use collections of tens when counting – either direct modeling or skip counting
Direct Place Value	<ul> <li>knows how many tens are in a number</li> <li>knows how much multiple groups of tens will be</li> <li>For example:</li> <li>*54. 5 tens is 50 and 4 more is 54"</li> </ul>

Carpenter, Thomas P., Fennema, E., Franke, M., Levi, L., Empson, S. (1999). Children's Mathematics: Cognitively Guided Instruction. Portsmouth, NH: Heinemann.