

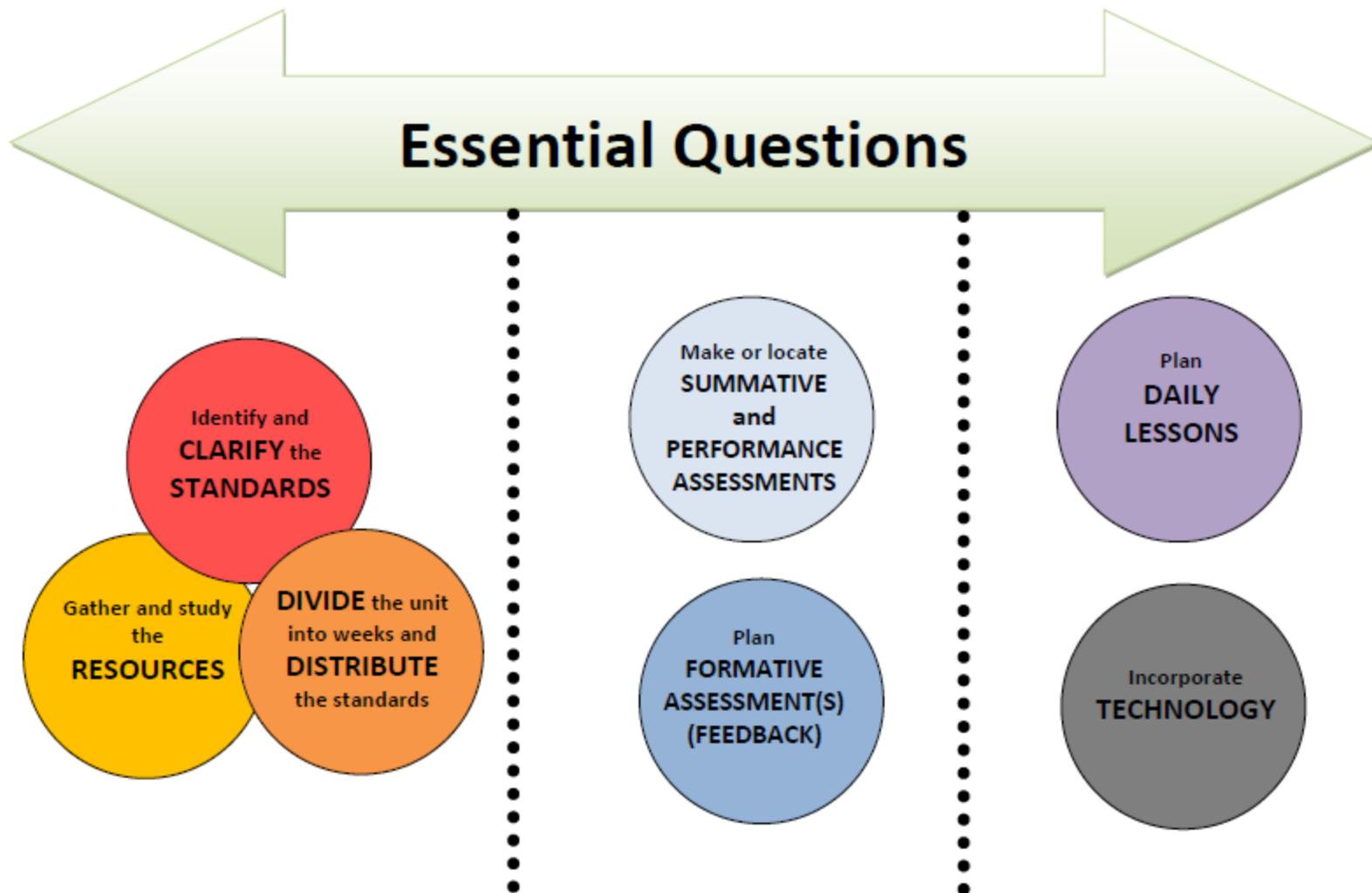
# Place Value and Operations with Decimals



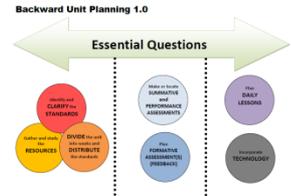
Unit Planning Team:

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Brooke Bradley (LW), Sharon Langston (FT)

# Backward Unit Planning 1.0



# Essential Questions



## Unit 3 – Place Value & Operations with Decimals

9 Weeks

Students will draw on their experiences with place value from grades two through four with whole number patterns and will be able to generalize those patterns in decimal numbers, namely the power of ten. As students work word problems with measurements in the metric system, where the same patterns occur, they begin to appreciate the value and meaning of decimals. Students will continue to develop their fluency with multi-digit multiplication. They continue building their strategies for multi-digit division. Students will add, subtract, multiply, and divide decimals to hundredths, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction.

### Essential Questions:

How can I take whole number patterns and what I know about base 10 fractions to generalize this understanding to decimal numbers?

How do the strategies we use related to the four operations apply to decimal numbers?

Number and Operations in Base Ten	
<b>Understand the place value system.</b>	
5.NBT.1	Recognize that in a multi-digit number, a digit in one place represents 10 times as much as it represents in the place to its right and 1/10 of what it represents in the place to its left.
5.NBT.2	Explain patterns in the number of zeros of the product when multiplying a number by powers of 10, and explain patterns in the placement of the decimal point when a decimal is multiplied or divided by a power of 10. Use whole-number exponents to denote powers of 10. Read, write, and compare decimals to thousandths.
5.NBT.3	a. Read and write decimals to thousandths using base-ten numerals, number names, and expanded form, e.g., $347.392 = 3 \times 100 + 4 \times 10 + 7 \times 1 + 3 \times (1/10) + 9 \times (1/100) + 2 \times (1/1000)$ . b. Compare two decimals to thousandths based on meanings of the digits in each place, using $>$ , $=$ , and $<$ symbols to record the results of comparisons.
5.NBT.4	Use place value understanding to round decimals to any place.
<b>Perform operations with multi-digit whole numbers and with decimals to hundredths.</b>	
5.NBT.5	Fluently multiply multi-digit whole numbers using the standard algorithm. <i>Minimum expectation: Standard algorithm is not expected to be applied until 4th quarter.</i>
5.NBT.6	Find whole-number quotients of whole numbers with up to four-digit dividends and two-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models.
5.NBT.7	Add, subtract, multiply, and divide decimals to hundredths, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used.
Measurement and Data	
<b>Convert like measurement units within a given measurement system.</b>	
5.MD.1	Convert among different-sized standard measurement units within a given measurement system (e.g., convert 5 cm to 0.05 m), and use these conversions in solving multi-step, real world problems.
Operations and Algebraic Thinking	
<b>Write and interpret numerical expressions.</b>	
<i>These standards will not be taught in isolated lessons, but will be addressed during Number Talks and Problem Solving discussion and notation.</i>	
5.OA.1	Use parentheses, brackets, or braces in numerical expressions, and evaluate expressions with these symbols.
5.OA.2	Write simple expressions that record calculations with numbers, and interpret numerical expressions without evaluating them. For example, express the calculation "add 8 and 7, then multiply by 2" as $2 \times (8 + 7)$ . Recognize that $3 \times (18932 + 921)$ is three times as large as $18932 + 921$ , without having to calculate the indicated sum or product.

**How can I take whole number patterns and what I know about base 10 fractions to generalize this understanding to decimal numbers?**

**How do the strategies we use related to the four operations apply to decimal numbers?**

# Background Knowledge

- Whole number place value understanding (How many 1s are in 10, how many 10s are in 100 etc.) Students can compare place values and explain patterns
- Base 10 fractions understanding ( $1/10$ ,  $1/100$ ,  $1/100$ )
- $a \div b = a/b$  What does this look like? 5 sharing 3 *When students can see the 3 divided into fifths.  $3/5$*
- Be able to name fractions parts: What is  $1/3$  of  $1/4$
- Experience with multiple groups, equal sharing, and base 10 problems
- Experience working with comparing fractions
- Experience with improper and mixed numbers- Students should be comfortable using both improper fractions and mixed numbers. The students should understand the relationship between the two and that both are correct ways of notating (How does this connect to decimals? Students will be better prepared write  $23/10$  as a decimal when they can reason about how many tenths it takes to make a whole.)

## Number and Operations in Base Ten

### Understand the place value system.

<b>5.NBT.1</b>	Recognize that in a multi-digit number, a digit in one place represents 10 times as much as it represents in the place to its right and 1/10 of what it represents in the place to its left.
<b>5.NBT.2</b>	Explain patterns in the number of zeros of the product when multiplying a number by powers of 10, and explain patterns in the placement of the decimal point when a decimal is multiplied or divided by a power of 10. Use whole-number exponents to denote powers of 10.
<b>5.NBT.3</b>	Read, write, and compare decimals to thousandths.
	<p>a. Read and write decimals to thousandths using base-ten numerals, number names, and expanded form, e.g., <math>347.392 = 3 \times 100 + 4 \times 10 + 7 \times 1 + 3 \times (1/10) + 9 \times (1/100) + 2 \times (1/1000)</math>.</p> <p>b. Compare two decimals to thousandths based on meanings of the digits in each place, using <math>&gt;</math>, <math>=</math>, and <math>&lt;</math> symbols to record the results of comparisons.</p>
<b>5.NBT.4</b>	Use place value understanding to round decimals to any place.

### Perform operations with multi-digit whole numbers and with decimals to hundredths.

<b>5.NBT.5</b>	Fluently multiply multi-digit whole numbers using the standard algorithm.
	<i>Minimum expectation: Standard algorithm is not expected to be applied until 4th quarter.</i>
<b>5.NBT.6</b>	Find whole-number quotients of whole numbers with up to four-digit dividends and two-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models.
<b>5.NBT.7</b>	Add, subtract, multiply, and divide decimals to hundredths, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used.

Use this language instead of adding or taking away zeros.

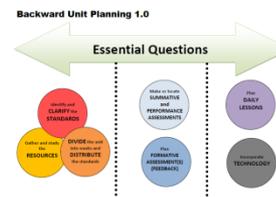
$$\begin{array}{|c|} \hline \# \text{ of} \\ \hline \text{groups} \\ \hline \end{array} \times \begin{array}{|c|} \hline \# \text{ in} \\ \hline \text{each} \\ \hline \text{group} \\ \hline \end{array} = \begin{array}{|c|} \hline \text{Total} \\ \hline \end{array}$$

This is the notion that is brought out in notation from 5.NBT. 1 and 5.NBT.2

This discussion really begins in unit 2 (Fractions to fractions) and continues to decimals. Number talks are a great way to being the conservations with decimals

Give them a reason to round...naked numbers do not give the students a reason to round. (Ex. Shopping scenarios, distance, use estimation)

Occurs daily in problem solving and number talks



**Identify and  
CLARIFY the  
STANDARDS**

## Measurement and Data

### Convert like measurement units within a given measurement system.

**5.MD.1** Convert among different-sized standard measurement units within a given measurement system (e.g., convert 5 cm to 0.05 m), and use these conversions in solving multi-step, real world problems.

## Operations and Algebraic Thinking

### Write and interpret numerical expressions.

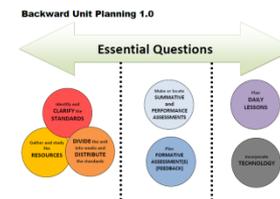
*These standards will not be taught in isolated lessons, but will be addressed during Number Talks and Problem Solving discussion and notation.*

**5.OA.1** Use parentheses, brackets, or braces in numerical expressions, and evaluate expressions with these symbols.

**5.OA.2** Write simple expressions that record calculations with numbers, and interpret numerical expressions without evaluating them. *For example, express the calculation "add 8 and 7, then multiply by 2" as  $2 \times (8 + 7)$ . Recognize that  $3 \times (18932 + 921)$  is three times as large as  $18932 + 921$ , without having to calculate the indicated sum or product.*

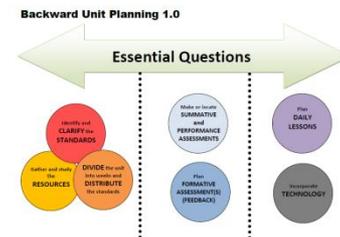
5. MD.1 Incorporate the metric system into decimal place value word problems.  
(NBT 1-2)

When students learn to reason about relationships on the reference sheet they will be able to use what they already know about multiplication and division to solve the problem. The focus should be on reasoning and relationships rather than just memorization. (NBT 5-7)



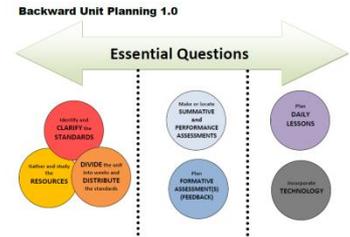
Identify and  
**CLARIFY** the  
**STANDARDS**

Week	Standards	Structure/Resources
1-2	<p>5.NBT.1 Recognize that in a multi-digit number, a digit in one place represents 10 times as much as it represents in the place to its right and 1/10 of what it represents in the place to its left.</p> <p>5.NBT.2 Explain patterns in the number of zeros of the product when multiplying a number by powers of 10, and explain patterns in the placement of the decimal point when a decimal is multiplied or divided by a power of 10. Use whole-number exponents to denote powers of 10.</p> <p>5.NBT.5</p> <p>5.NBT.6</p> <p>5.NBT.7 These operations will come out during our problem solving discussions/strategies</p> <p>5.MD.1 Convert among different-sized standard measurement units within a given measurement system (e.g., convert 5 cm to 0.05 m), and use these conversions in solving multi-step, real world problems.</p> <p>Bring out 5.OA.1 &amp; 5.OA.2 in discussions</p>	<ul style="list-style-type: none"> <li>•Alternate between multiplication and measurement division using both whole numbers and decimals ( we are merging our ideas of whole numbers and fractions in this unit)</li> <li>•The number in the <b># in each group</b> needs to be a power of ten ( 10, 100, 0.1, 0.01)</li> </ul> <div style="text-align: center; border: 1px solid black; padding: 5px; margin: 10px 0;"> <math display="block">\boxed{\text{\# of groups}} \times \boxed{\text{\# in each group}} = \boxed{\text{Total}}</math> </div> <ul style="list-style-type: none"> <li>•Introduce decimal notation</li> <li>•See Chapter 7 in ECM book (listed on Rogers site) <ul style="list-style-type: none"> <li>•Week 1: Animal at the Zoo pg. 154</li> <li>•Week 2: Multiplication problem (cupcakes and frosting)</li> </ul> </li> </ul> <p>(these problems and discussion will take multiple days)</p> <p><i>Students need experience with both contextual problems and problems without context</i></p> <ul style="list-style-type: none"> <li>•Measurement introduction: Could use <u>Millions to Measure</u> by David M Schwartz</li> <li>•<b>Number talk ideas:</b>  Bundling base ten problems: <ul style="list-style-type: none"> <li>• How many tens are 57? How many tens are in 243? (Good time to work on notation)</li> <li>•How many tenths are in 387.09? How many tens are in 387.09?</li> </ul> </li> </ul>



**DIVIDE the unit into weeks and DISTRIBUTE the standards**

Week	Standards	Structure/Resources
3	<p>5.NBT.1 5.NBT.2</p> <p>5.NBT.5 5.NBT.6 5.NBT.7 These operations will come out during our problem solving discussions/strategies</p> <p>5.MD.1 Convert among different-sized standard measurement units within a given measurement system (e.g., convert 5 cm to 0.05 m), and use these conversions in solving multi-step, real world problems.</p> <p>Bring out 5.OA.1 &amp; 5.OA.2 in discussions</p>	<ul style="list-style-type: none"> <li>•Alternate between multiplication and measurement division using both whole numbers and decimals ( we are merging our ideas of whole numbers and fractions in this unit)</li> <li>•Continue decimal notation</li> <li>•See Chapter 7 in ECM book (listed on Rogers site) <ul style="list-style-type: none"> <li>•Mellery’s Chili pg. 164</li> </ul> </li> <li>(the number sets should include whole numbers and decimals)</li> <li><i>Students need experience with both contextual problems and problems without context</i></li> <li>•<b><u>Number talk ideas:</u></b> <ul style="list-style-type: none"> <li>• ECM book pg. 173</li> </ul> </li> <li>•Continue measurement problems pulling context and characters from <u>Millions to Measure</u></li> </ul>



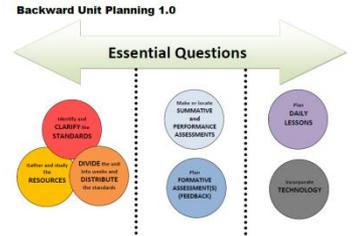
**DIVIDE** the unit  
into weeks and  
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the standards

Week	Standards	Structure/Resources
4	<p>5.NBT.3 Read, write, and compare decimals to thousandths.</p> <p>a. Read and write decimals to thousandths using base-ten numerals, number names, and expanded form, e.g., <math>347.392 = 3 \times 100 + 4 \times 10 + 7 \times 1 + 3 \times (1/10) + 9 \times (1/100) + 2 \times (1/1000)</math>.</p> <p>b. Compare two decimals to thousandths based on meanings of the digits in each place, using <math>&gt;</math>, <math>=</math>, and <math>&lt;</math> symbols to record the results of comparisons.</p> <p>5.NBT.5</p> <p>5.NBT.6</p> <p>5.NBT.7 These operations will come out during our problem solving discussions/strategies</p> <p>5.MD.1 (1 day this week) Bring out 5.OA.1 &amp; 5.OA.2 in discussions</p>	<p>Alternate between multiplication and measurement division using both whole numbers and decimals ( we are merging our ideas of whole numbers and fractions in this unit)</p> <ul style="list-style-type: none"> <li>•Continue decimal notation</li> <li>•See Chapter 7 in ECM book (listed on Rogers site) <ul style="list-style-type: none"> <li>•Intravenous Drip pg. 169</li> <li>•Papa Pete’s Pizza Place (on website)</li> </ul> </li> </ul> <p><i>Students need experience with both contextual problems and problems without context</i></p> <p>•<b><u>Number talk ideas:</u></b></p> <ul style="list-style-type: none"> <li>•Comparing decimals</li> <li>•Continue measurement problems pulling context and characters from <u><i>Millions to Measure</i></u></li> </ul>



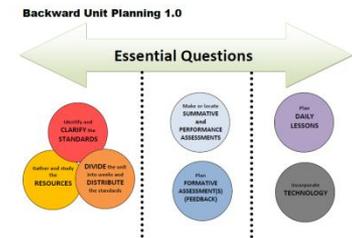
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Week	Standards	Structure/Resources
5	<p>5.NBT.3  a. Read and write decimals to thousandths using base-ten numerals, number names, and expanded form, e.g., <math>347.392 = 3 \times 100 + 4 \times 10 + 7 \times 1 + 3 \times (1/10) + 9 \times (1/100) + 2 \times (1/1000)</math>.  b. Compare two decimals to thousandths based on meanings of the digits in each place, using <math>&gt;</math>, <math>=</math>, and <math>&lt;</math> symbols to record the results of comparisons.</p> <p>5.NBT.4 Use place value understanding to round decimals to any place.</p> <p>5.NBT.5</p> <p>5.NBT.6</p> <p>5.NBT.7 These operations will come out during our problem solving discussions/strategies</p> <p>5.MD.1 (1 day this week)  Bring out 5.OA.1 &amp; 5.OA.2 in discussions</p>	<p>Alternate between multiplication and measurement division using both whole numbers and decimals ( we are merging our ideas of whole numbers and fractions in this unit)</p> <ul style="list-style-type: none"> <li>•Continue decimal notation</li> <li>•Problems to pose <ul style="list-style-type: none"> <li>•Applesauce Jars (website)</li> <li>•Water Challenge (website) Use to bring in rounding and multiplication</li> </ul> </li> </ul> <p><i>Students need experience with both contextual problems and problems without context</i></p> <ul style="list-style-type: none"> <li>•<b><u>Number talk ideas:</u></b></li> <li>•Comparing decimals, whole numbers, and fractions</li> </ul> <ul style="list-style-type: none"> <li>•Continue measurement problems pulling context and characters from <u>Millions to Measure</u></li> </ul>



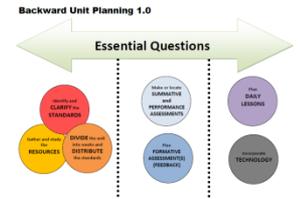
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Week	Standards	Structure/Resources
6	<p>5.NBT.3</p> <p>a. Read and write decimals to thousandths using base-ten numerals, number names, and expanded form, e.g., <math>347.392 = 3 \times 100 + 4 \times 10 + 7 \times 1 + 3 \times (1/10) + 9 \times (1/100) + 2 \times (1/1000)</math>.</p> <p>b. Compare two decimals to thousandths based on meanings of the digits in each place, using <math>&gt;</math>, <math>=</math>, and <math>&lt;</math> symbols to record the results of comparisons.</p> <p>5.NBT.4 Use place value understanding to round decimals to any place.</p> <p>5.NBT.5</p> <p>5.NBT.6</p> <p>5.NBT.7 These operations will come out during our problem solving discussions/strategies</p> <p>5.MD.1 (1 day this week) Bring out 5.OA.1 &amp; 5.OA.2 in discussions</p>	<p>This would be a good time to do an interim assessment to see where your students are with the standards.</p> <p>Problems to pose:</p> <ul style="list-style-type: none"> <li>•Addition: The Daring Divers (website)</li> </ul> <p><i>Students need experience with both contextual problems and problems without context</i></p> <p>•<b><u>Number talk ideas:</u></b></p> <ul style="list-style-type: none"> <li>•Continue measurement problems pulling context and characters from <u>Millions to Measure</u></li> </ul>



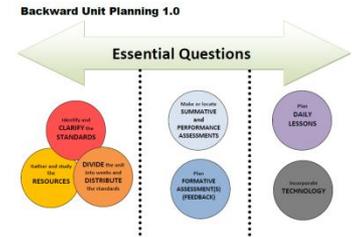
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Week	Standards	Structure/Resources
7	<p>5.NBT.5 5.NBT.6 5.NBT.7 These operations will come out during our problem solving discussions/strategies</p> <p>5.MD.1 (1 day this week) Bring out 5.OA.1 &amp; 5.OA.2 in discussions</p>	<p>If your students are ready to move forward:</p> <p>Problems to pose:</p> <ul style="list-style-type: none"> <li>•Problems to pose with Rate (website)</li> <li>•Pose multiplication and division problems</li> <li>•Order of Operation problems with decimals included and/or a rectangular prism with L,W, and H with decimals.</li> </ul> <p>Website Resources: Bowling for Numbers Watch Out for Parentheses 1, Comparing Products Video Game Scores Words to Expressions 1</p> <p>Pose Problem with conversions in the metric system</p>



**DIVIDE** the unit into weeks and **DISTRIBUTE** the standards

Week	Standards	Structure/Resources
8	5. NBT. 3 5. NBT. 4 5. NBT. 7  5.MD.1	<ul style="list-style-type: none"> <li>•Continue to discuss decimals in both contextual and <b>non contextual</b> problems. The technology resources on the website include decimal open number sentences that would be great examples of non contextual problems.</li> <li>•Continue number talks; supplemental number talks for unit 3 (website)</li> <li>•The Deep Curriculum Alignment Project for Mathematics Sample Task located on the website has great questions to use to check for deep understanding.</li> <li>•Continue work with conversions.</li> <li>*If you see students continuing to struggle with certain aspects- you could use the games and activities for whole group while you pull students back for interventions.</li> </ul>
9	All Standards	<ul style="list-style-type: none"> <li>•Teachers could use Decimal Choice Boards during Week 9 to offer differentiation and this will provide small group opportunities before the assessment</li> <li>•Continue lessons from week 8</li> <li>•End with an assessment</li> </ul>



**DIVIDE** the unit  
into weeks and  
**DISTRIBUTE**  
the standards



- Planning Options
- Lesson Resources**
- Technology Resources
- Games and Activities
- Number Talks for Unit 3
- Assessments
- Teacher Created Resources for Unit 3

Intranet » K-5 Curriculum » 5th Grade Curriculum » Math » Curricular and Instructional Resources » U3: Place Value and Operations with Decimals » Lesson Resources

### Lesson Resources



Problem Situations for Decimals (5.NBT.7)

Problems to Pose for Decimals with Rate (5.NBT.7)

Problems to Pose to Promote Base 10 Understanding (5.NBT.1)



**Extending Children's Mathematics: Fractions and Decimals**  
by Susan B. Empson and Linda Levi  
Chapters 7 and 8 apply to this unit.  
Decimal Place Value and Operations Resource guide for using ECM book  
(5.NBT.1, 5.NBT.2, 5.NBT.3, 5.NBT.4, 5.NBT.7)  
Instructional Progression of Fraction and Decimal Operations

**Student Recording Sheets** for problems found in "From the Classroom: Teaching Decimals" (Chapter 7) The following documents are student recording sheets for problems presented in Chapter 7. (5.NBT.1, 5.NBT.2)  
**Animal at the Zoo** "Chapter Showcase Problem" (p. 154-159)  
**Mellery's Chili** (p. 164)  
**Intravenous Drip** (p. 169)



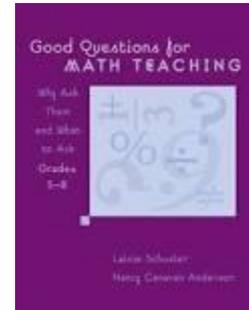
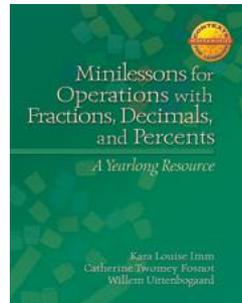
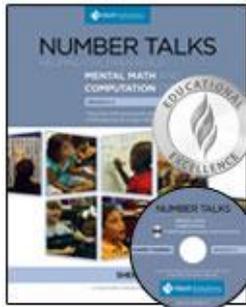
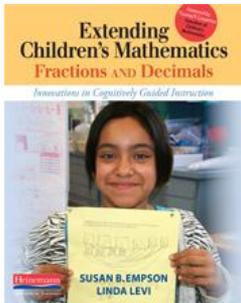
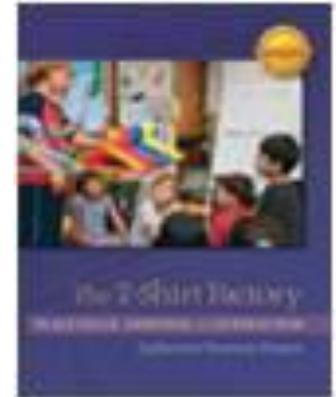
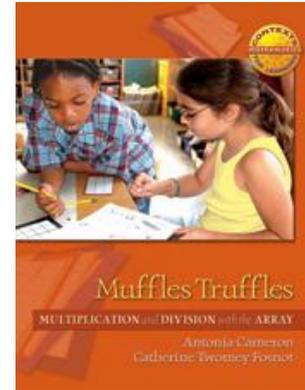
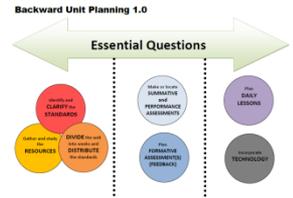
**Minilessons for Operations with Fractions, Decimals, & Percents** This book contains minilessons that you can choose from as you consider the needs of your students and can be used throughout the school year. These are more guided and explicit and were designed to be used at the start of your math instruction - lasting 10 to 15 minutes. See the overview (p. 5-12) for further details about the minilessons.  
*Minilessons addressing decimals can be found on pages 65, 74, 82-85.*

**Contextual Problem Solving Situations** In the tasks below, students will develop their understanding of whole number and decimal operations through contextual situations.

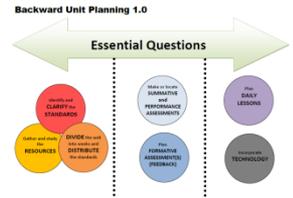
**Tasks Addressing 5.NBT.1**

- Conserving Cookies
- Applesauce Jars
- Intravenous Drip
- Boxes of Candy Word Document SMART Notebook
- Pounds of Clay Word Document SMART Notebook
- Tasks Addressing 5.NBT.2**
- Babysitting

# Gather and study the RESOURCES



# Options for Assessment – available online for Unit 2



Name: \_\_\_\_\_ Date: \_\_\_\_\_

### Unit 3 – Place Value and Operations with Decimals (5.MD.1)

Write  $>$ ,  $<$ , or  $=$  in the circle to compare the measurements.

$3 \frac{1}{2}$  hours  200 minutes

3 quarts  6 cups

5 kilometers  5,000 meters

35 feet  11 yards

Choose two of your solutions above and explain your thinking.

\_\_\_\_\_

\_\_\_\_\_

\_\_\_\_\_

\_\_\_\_\_

Name: \_\_\_\_\_ Date: \_\_\_\_\_

### Unit 3 – Place Value and Operations with Decimals (5.MD.1)

In the long jump, Karen can jump 51 inches, Debbie can jump 4 feet 4 inches, and Margaret can jump 1 yard, 1foot, 1 inch. Who can jump the farthest?

Use what you know about customary measurement to explain how you found your answer.

\_\_\_\_\_

\_\_\_\_\_

\_\_\_\_\_

\_\_\_\_\_

Make or locate  
**SUMMATIVE**  
and  
**PERFORMANCE**  
**ASSESSMENTS**

Name: \_\_\_\_\_ Date: \_\_\_\_\_

### Unit 3 – Place Value and Operations with Decimals

Round the following numbers to the nearest hundredth.

	Round to hundredth
5.025	
5.079	
5.103	
5.117	
5.108	

Solve

a.  $0.35 \times 1.5 =$

b.  $5.63 + 14.37 =$

c.  $371 \times 2,584 =$

d.  $625 \times 847 =$

e.  $85.703 + 12.197 =$

f.  $57.03 + 2.08 =$

g.  $0.3 + 0.82 =$

h.  $1.4 - 0.7 =$

i.  $7.148 - 0.07 =$

Name: \_\_\_\_\_ Date: \_\_\_\_\_

### Unit 3 – Place Value and Operations with Decimals (5.NBT.1, 5.NBT.3)

1. Express as decimal numerals.

a. three thousandths	
b. thirty-four thousandths	
c. five hundred and seven hundredths	
d. $\frac{26}{1000}$	
e. $3 \frac{94}{100}$	

2. Express each of the following values in words.

a. 0.006

\_\_\_\_\_

b. 12.056

\_\_\_\_\_

c. 205.68

\_\_\_\_\_

3. Write the number in expanded form using fractions or decimals to express the decimal place value units.

a. 24.73

\_\_\_\_\_

b. 0.239

\_\_\_\_\_

4. Write a decimal for each of the following.

a.  $7 \times 10 + 3 \times 1 + 6 \times (\frac{1}{10}) + 8 \times (\frac{1}{100})$

\_\_\_\_\_

b.  $4 \times 100 + 2 \times 10 + 7 \times 0.1 + 9 \times 0.001$

\_\_\_\_\_



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