Connecting Whole Number Operations Addition & Subtraction of Mixed Numbers; Multiplicative Comparison

4<sup>th</sup> Grade Unit 3



Unit Planning Team: Angela Black (ES), Rea Smith (RG), Susan Harp (JD), Haylee Pierce (JM), Wes Faith (JM)

## Connecting Whole Number Operations Addition & Subtraction of Mixed Numbers; Multiplicative Comparison

4<sup>th</sup> Grade Unit 3



The main focus of third quarter involves the introduction of **multiplicative comparisons**. In third grade, students studied multiplication as equal groups, arrays, and area; in fourth grade, students extend this understanding using multiplicative comparisons. They will use their understanding of multiplicative comparison to solve problems involving measurement and conversions from a larger unit to a smaller unit. Students continue to work with all four operations using whole numbers. They will extend multiplication to multiplying two two-digit numbers and division up to a four-digit dividend by a one-digit divisor. Students continue to develop strategies using their base-ten understanding along with meanings and properties of operations, to compute with whole numbers. Students build on their work from second quarter to add and subtract fractions with like denominators, as well as multiply fractions by a whole number. They extend this knowledge to include adding and subtracting mixed numbers with like denominators. Contexts for problem-solving that support the major work of this quarter include solving whole number multi-step problems and real-world scenarios with simple fractions, as well as measurement conversions.

### **Backward Unit Planning 1.0**



### **Essential Questions**





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#### R.P.S. Common Core Math Curriculum

4th Grade

### ${\bf 3}^{rd}$ Quarter $_{(p.\,1\,of\,2)}$ Connecting Whole Number Operations to Addition & Subtraction of Mixed Numbers and Multiplicative Comparison

The main focus of third quarter involves the introduction of multiplicative comparisons. In Third grade, students studied multiplication as equal groups, arrays, and area; in fourth grade, students extend this understanding using multiplicative comparisons. They will use their understanding of multiplicative comparison to solve problems involving measurement and conversions from a larger unit to a smaller unit. Students continue to work with all four operations using whole numbers. They will extend multiplication to multiplying two two-digit numbers and division up to a four-digit dividend by a one-digit divisor. Students continue to develop strategies using their base-ten understanding along with meanings and properties of operations, to compute with whole numbers. Students build on their work from second quarter to add and subtract fractions with like denominators, as well as multiply fractions by a whole number. They extend this knowledge to include adding and subtracting mixed numbers with like denominators. Contexts for problem-solving that support the major work of this quarter include solving whole number multi-step problems and real-world scenarios with simple fractions, as well as measurement conversions.

	Operations and Algebraic Thinking
Use the fo	our operations with whole numbers to solve problems.
4.0A.1	Interpret a multiplication equation as a comparison, e.g., interpret $35 = 5 \times 7$ as a statement that $35$ is 5 times as many as 7 and 7 times as many as 5. Represent verbal statements of multiplicative comparisons as multiplication equations.
4.OA.2	Multiply or divide to solve word problems involving multiplicative comparison, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem, distinguishing multiplicative comparison from additive comparison.
4.OA.3	Solve multistep word problems posed with whole numbers and having whole-number answers using the four operations, including problems in which remainders must be interpreted. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.
Generate	and analyze patterns.
4.OA.5	Generate a number or shape pattern that follows a given rule. Identify apparent features of the pattern that were not explicit in the rule itself. For example, given the rule "Add 3" and the starting number 1, generate terms in the resulting sequence and observe that the terms appear to alternate between odd and even numbers. Explain informally why the numbers will continue to alternate in this way.
	Number and Operations in Base Ten (expectations in this domain are limited to whole numbers less than or equal to 1,000,000)
Use place	value understanding and properties of operations to perform multi-digit arithmetic.
4.NBT.4	Fluently add and subtract multi-digit whole numbers using the standard algorithm.
4.NBT.5	Multiply a whole number of up to four digits by a one-digit whole number, and multiply two two- digit numbers, using strategies based on place value and the properties of operations. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models.
4.NBT.6	Find whole-number quotients and remainders with up to four-digit dividends and one-digit divisors, using strategies based on place value, the properties of operations, and/or the relationship between multiplication and division. Illustrate and explain the calculation by using equations, rectangular arrays, and/or area models.

### **New Essential Questions:**

How do I use comparisons to reason about size and quantity?

How can I use what I know about whole numbers to help me understand fraction operations?

	<b>Operations and Algebraic Thinking</b>		
Use the fo	our operations with whole numbers to solve problems.		
4.0A.1	Interpret a multiplication equation as a comparison, e.g., interpret 35 = 5 × is 5 times as many as 7 and 7 times as many as 5. Represent verbal stateme comparisons as multiplication equations.		Clarifications of Reoccurring
4.OA.2	Multiply or divide to solve word problems involving multiplicative comparis drawings and equations with a symbol for the unknown number to represe distinguishing multiplicative comparison from additive comparison.	m	Ongoing throughout the year; Include
4.0A.3	Solve multistep word problems posed with whole numbers and having who the four operations, including problems in which remainders must be inter problems using equations with a letter standing for the unknown quantity. reasonableness of answers using mental computation and estimation strate	4.0A.3	include letters standing for unknown quantities; Connect to problems types that involve comparison
Generate	and analyze patterns.		Continued maintenance with addition and
4.OA.5	Generate a number or shape pattern that follows a given rule. Identify apppertern that were not explicit in the rule itself. For example, given the rule number 1, generate terms in the resulting sequence and observe that the ter between odd and even numbers. Explain informally why the numbers will contain this way.	4.NBT.4	subtraction; Small group instruction for students who struggle; Work with base ten and counting within base ten; Students should be working toward a standard
	Number and Operations in Base Ten (expectations in this domain are limited to whole numbers less than or equal to		algorithm by the end of the year; Use problem types involving additive comparison
Use place	value understanding and properties of operations to perform multi-digit a	Ŀ.	4 x 1 and 2 x 2; Illustrate through equations,
4.NBT.4	Fluently add and subtract multi-digit whole numbers using the standard alg	NBJ	rectangular arrays, and area models based on
4.NBT.5	Multiply a whole number of up to four digits by a one-digit whole number, digit numbers, using strategies based on place value and the properties of explain the calculation by using equations, rectangular arrays, and/or area	T.6 4.1	Up to 4 divided by 1; inverse of 4.NBT.5
4.NBT.6	Find whole-number quotients and remainders with up to four-digit dividen using strategies based on place value, the properties of operations, and/or multiplication and division. Illustrate and explain the calculation by using eq arrays, and/or area models.	A N N N N N N N N N N N N N N N N N N N	ctangular



	<b>Number and Operations - Fractions</b> (expectations in this domain are limited to fractions with denominators 2,3,4,5,6,8,10,12, and 100)		
Build frac	tions from unit fractions by applying and extending previous understandings of operations on whole nu	ımbers.	
	Understand a fraction a/b with a > 1 as a sum of fractions 1/b.		
	<b>b.</b> Decompose a fraction into a sum of fractions with the same denominator in more than one way, record decomposition by an equation. Justify decompositions, e.g., by using a visual fraction model. <i>Examples:</i> $3/8 = 1/8 + 1/8 + 1/8 = 3/8 = 1/8 + 2/8 = 2 + 1/8 = 1 + 1 + 1/8 = 8/8 + 8/8 + 1/8$ .	rding each	Clarifications of Reasourring
4.NF.3	<b>c.</b> Add and subtract mixed numbers with like denominators, e.g., by replacing each mixed number with and/or by using properties of operations and the relationship between addition and subtraction.		Standards
	<b>d.</b> Solve word problems involving addition and subtraction of fractions referring to the same whole and denominators, e.g., by using visual fraction models and equations to represent the problem.		Part "a" has dropped off and "c" has been
	Apply and extend previous understandings of multiplication to multiply a fraction by a whole number.	ŝ	added (+/- mixed numbers); Involves
4.NF.4	<b>b.</b> Understand a multiple of $a/b$ as a multiple of $1/b$ , and use this understanding to multiply a fraction b example, use a visual fraction model to express $3 \times (2/5)$ as $6 \times (1/5)$ , recognizing this product as $6/5$ . (In a)/b.)	4.NF	flexibility and decomposing fractions different ways; All work involves like denominators
	<b>c.</b> Solve word problems involving multiplication of a fraction by a whole number, e.g., by using visual fraequations to represent the problem. For example, if each person at a party will eat 3/8 of a pound of robe 5 people at the party, how many pounds of roast beef will be needed? Between what two whole num lie?	NF.2	Fraction equivalence and comparison are not in the pacing for this quarter, but will need to
Understa	nd decimal notation for fractions, and compare decimal fractions.	4.	be continued as you work with fractions
4.NF.5	Express a fraction with denominator 10 as an equivalent fraction with denominator 100, and use this te fractions with respective denominators 10 and 100.4 <i>For example, express 3/10 as 30/100, and add 3/1</i>	NF.1/	
	Measurement and Data	4.	
Solve pro	blems involving measurement and conversion of measurements from a larger unit to a smaller unit.		
4.MD.1	Know relative sizes of measurement units within one system of units including km, m, cm; kg, g; lb, oz.; Within a single system of measurement, express measurements in a larger unit in terms of a smaller un equivalents in a two column table. For example, know that 1 ft is 12 times as long as 1 in. Express the le. 48 in. Generate a conversion table for feet and inches listing the number pairs (1, 12), (2, 24), (3, 36),	4.NF.4	distributive and associative properties- fraction by a whole number; "c" pertains to
	Use the four operations to solve word problems involving distances, intervals of time, liquid volumes, m		manuple groups problems
4.MD.2	money, including problems involving simple fractions or decimals, and problems that require expressing a larger unit in terms of a smaller unit. Represent measurement quantities using diagrams such as numl feature a measurement scale.	ID.2	Involves all four operations; bring in conversions and fractions to solve within
Quart	terly Expectation: Problems posed should involve measurement quantities with fractions and conversions.	Σ	measurement contexts; Measurement scale
4.MD.3	Apply the area and perimeter formulas for rectangles in real world and mathematical problems. For exc a rectangular room given the area of the flooring and the length, by viewing the area formula as a multian unknown factor.	4	refers to number lines



	<b>Operations and Algebraic Thinking</b>		
Use the fo	our operations with whole numbers to solve problems.		
4.0A.1	Interpret a multiplication equation as a comparison, e.g., interpret 35 = 5 × 7 is 5 times as many as 7 and 7 times as many as 5. Represent verbal statement comparisons as multiplication equations.	as a stater	nent that 35
4.OA.2	Multiply or divide to solve word problems involving multiplicative compariso drawings and equations with a symbol for the unknown number to represen distinguishing multiplicative comparison from additive comparison.		Standards
4.OA.3	Solve multistep word problems posed with whole numbers and having whole the four operations, including problems in which remainders must be interpr problems using equations with a letter standing for the unknown quantity. <i>A</i> reasonableness of answers using mental computation and estimation strateg	I.0A.1	"as much as" and "times as many" vocabulary from progressions; moving from equal groups in previous grades to multiplicative comparison (connects to
Generate	and analyze patterns.	ч	4.NBT.1 standard of 10xs as many with place
4.OA.5	Generate a number or shape pattern that follows a given rule. Identify appar pattern that were not explicit in the rule itself. For example, given the rule ". number 1, generate terms in the resulting sequence and observe that the tern between odd and even numbers. Explain informally why the numbers will cor this way.	A.2	value); Use Problem Types Chart Multiplication and division word problems that involve multiplicative comparison; Distinguish multiplicative from additive
E.	<b>Number and Operations in Base Ten</b> (expectations in this domain are limited to whole numbers less than or equal to 1	4.0/	comparison when beginning work with comparison this quarter
Use place	value understanding and properties of operations to perform multi-digit ari		
4.NBT.4	Fluently add and subtract multi-digit whole numbers using the standard algo		Involves number and shape patterns:
4.NBT.5	Multiply a whole number of up to four digits by a one-digit whole number, a digit numbers, using strategies based on place value and the properties of or explain the calculation by using equations, rectangular arrays, and/or area m	4.0A.5	Number patterns can connect to additive and multiplicative comparison, making sure to address the rule when working with patterns
4.NBT.6	Find whole-number quotients and remainders with up to four-digit dividends using strategies based on place value, the properties of operations, and/or the multiplication and division. Illustrate and explain the calculation by using equ arrays, and/or area models.	s and one-d ne relations lations, red	ligit αivisors, hip between tangular



	<b>Number and Operations - Fractions</b> (expectations in this domain are limited to fractions with denominators 2,3,4,5,6,8,10,12, and 100)		
Build frac	tions from unit fractions by applying and extending previous understandings of operations on whole num	ıbers.	
	Understand a fraction a/b with a > 1 as a sum of fractions 1/b. <b>b.</b> Decompose a fraction into a sum of fractions with the same denominator in more than one way, recondecomposition by an equation. Justify decompositions, e.g., by using a visual fraction model. <i>Examples: 3/8 = 1/8 + 1/8 + 1/8 ; 3/8 = 1/8 + 2/8 ; 2 1/8 = 1 + 1 + 1/8 = 8/8 + 8/8 + 1/8</i> .		Clarifications of New Standards
4.NF.3	<b>c.</b> Add and subtract mixed numbers with like denominators, e.g., by replacing each mixed number with ar and/or by using properties of operations and the relationship between addition and subtraction.		Refer to Chapter 7 in the ECM book; ties to
	<b>d.</b> Solve word problems involving addition and subtraction of fractions referring to the same whole and h denominators, e.g., by using visual fraction models and equations to represent the problem.	Ŀ.	4.NF.1 with equivalent fractions; could tie into money using pennies and dimes; can tie
	Apply and extend previous understandings of multiplication to multiply a fraction by a whole number.	Z	into multiplicative comparisons with
4.NF.4	<b>b.</b> Understand a multiple of $a/b$ as a multiple of $1/b$ , and use this understanding to multiply a fraction by example, use a visual fraction model to express $3 \times (2/5)$ as $6 \times (1/5)$ , recognizing this product as $6/5$ . (In g a)/b.)	4.	converting between tenths and hundredths; Use base-ten blocks and equal sharing to reinforce this idea
	<b>c.</b> Solve word problems involving multiplication of a fraction by a whole number, e.g., by using visual fractequations to represent the problem. For example, if each person at a party will eat 3/8 of a pound of roas be 5 people at the party, how many pounds of roast beef will be needed? Between what two whole number lie?	сi	Conversions; Idea- Use a two column table to show conversions connecting to 4.OA.5;
Understa	nd decimal notation for fractions, and compare decimal fractions.	Ō	Metric and customary units; Lies into
4.NF.5	Express a fraction with denominator 10 as an equivalent fraction with denominator 100, and use this tech fractions with respective denominators 10 and 100.4 For example, express 3/10 as 30/100, and add 3/10	4.N	multiplicative comparison when converting
	Measurement and Data		
Solve pro	blems involving measurement and conversion of measurements from a larger unit to a smaller unit.		Area and navimator formula in real world
4.MD.1	Know relative sizes of measurement units within one system of units including km, m, cm; kg, g; lb, oz.; l, Within a single system of measurement, express measurements in a larger unit in terms of a smaller unit. equivalents in a two column table. For example, know that 1 ft is 12 times as long as 1 in. Express the leng 48 in. Generate a conversion table for feet and inches listing the number pairs (1, 12), (2, 24), (3, 36),	4.MD.3	problems; Could have missing side lengths; Rich Lehrer area measure resource
4.MD.2	Use the four operations to solve word problems involving distances, intervals of time, liquid volumes, ma- money, including problems involving simple fractions or decimals, and problems that require expressing r a larger unit in terms of a smaller unit. Represent measurement quantities using diagrams such as numbe feature a measurement scale.		
Quart	terly Expectation: Problems posed should involve measurement quantities with fractions and conversions.		
4.MD.3	Apply the area and perimeter formulas for rectangles in real world and mathematical problems. For example a rectangular room given the area of the flooring and the length, by viewing the area formula as a multipli an unknown factor.	ple, find the v cation equati	vidth of on with



Week	Standards	Explanation/Clarification	Backward Unit Planning 1.0
1	Focus 4.OA.1 / 4.OA.2 4.NF.4 Connection 4.NBT.1 (not actually paced for this quarter) Continuous 4.NBT.5/4.NBT.6 4.OA.3	Understanding the difference between multiplicative and additive comparison Relating multiplicative comparison to the relationship to base ten (4.NBT.1 Recognize that in a multi-digit whole number, a digit in one place represents 10xs what it represents in the place to its right) Continue to develop strategies based on place value and properties of operations	Essential Questions
2	Focus 4.OA.1 / 4.OA.2 4.NF.4 Connection 4.NBT.1 (not actually paced for this quarter) Continuous 4.NBT.5/4.NBT.6 4.OA.3	Continue with same focus as week 1	the standards
3	Focus 4.MD1/4.MD.2 4.OA.5 Connection 4.OA.1/4.OA.2 Continuous 4.NBT.4/4.NBT.5/4NBT.6 4.OA.3	Use understanding of multiplicative comparisons in the context of problems involving measurement conversions connect to 4.OA.5 in working with the patterns that evolve from measurement conversions	

Week	Standards	Explanation/Clarification
4	Focus 4.MD1/4.MD.2 4.OA.5 Connection 4.OA.1/4.OA.2 Continuous 4.NBT.4/4.NBT.5/4NBT.6 4.OA.3	Continue work from week 3 4.OA.5- extend pattern work to other shape and number patterns with rules
5	Focus 4.NF.5 4.MD.1 Connection 4.OA1/4.OA.2 Continuous 4.NBT.1 (not in this quarter pacing) 4.NBT.4/4.NBT.5/4.NBT.6 4.OA.3	In order to understand the multiplicative relationship between 3/10 and 30/100 (4.NF.5), you must understand the multiplicative nature of our base ten system (4.NBT.1) 1 is ten times as much as 1/10 and 1/10 is ten times as much as 1/100 This understanding can connect to 4.MD.1 when converting in the metric system
6	Focus 4.NF.5 4.MD.1 Connection 4.OA.1/4.OA.2 Continuous 4.NBT.1 (not in this quarter pacing) 4.NBT.4/4.NBT.5/4.NBT.6 4.OA.3	Same as week 5

			Backward Unit Planning 1.0
Week	Standards	Explanation/Clarification	Essential Questions
7	Focus 4.NF.3/4.NF.4 Continuous 4.NBT.4/4.NBT.5/4NBT.6 4.OA.3 4.OA.1/4.OA.2	<ul> <li>4.NF.3 could be used to push additive comparison with fractional amounts; mixed numbers have been added to this quarter; subtraction of fractions should be a focus, if it hasn't been yet</li> <li>4.NF.4 relates to multiplicative comparison as in ¾ is the same as 3 times as much as ¼; should also focus on multiple groups problems as in ¾ is the same as 3 groups of ¼</li> </ul>	DIVIDE the unit into weeks and
8	Focus 4.NF.3/4.NF.4 Continuous 4.NBT.4/4.NBT.5/4NBT.6 4.OA.3 4.OA.1/4.OA.2	Same as week 8	the standards
9	Focus 4.MD.3 Connection 4.MD.2 Continuous 4.NBT.4/4.NBT.5/4NBT.6 4.OA.3	<ul> <li>4.MD.3 is an application of the area and perimeter formulas for rectangles and assumes that students have had sufficient time exploring and building understanding of those formulas if you feel that your students do not have this understanding, you may need to devote more time throughout the quarter to explore these ideas</li> <li>Comparison can be a context when comparing area and perimeter of different rectangles</li> </ul>	

## Suggested Weekly Posing of Problems:

This is one way to think about clustering the standards. These ideas would be repeated each week.

**Essential Questions** 

- 1) How do I use comparisons to reason about size and quantity?
- 2) How can I use what I know about whole numbers to help me understand fraction operations?
- 1-2 days a week- (4.NBT.4, 4.NF.3, 4.OA.3)

Focus on <u>additive</u> comparison problems to revisit whole number addition and subtraction (EQ 1) as well as adding and subtracting fractions (EQ 2). Include multi-step problems.

**2-3 days a week-** Focus on <u>multiplicative</u> comparison problems (EQ 1). Connections should be made to base 10 understanding and measurement conversions. Pose multiplication of a fraction by a whole number. (4.OA.1, 4.OA.2, 4.MD.1, 4.MD.2, 4.OA.5, 4.NBT.5, 4.NBT.6, 4.NF.5)

**1-2 days a week-** Compare rectangular areas (EQ 1) (4.MD.3)



DIVIDE the unit into weeks and DISTRIBUTE the standards

# COMMON

#### SHIFTS FOR MATHEMATICS

- Focus strongly where the standards focus.
- Coherence: think across grades, and link to major topics within grades.
- Rigor: in major topics, pursue conceptual understanding, procedural skill and fluency, and application.



Problems p.32-35

Instructional Guidelines for Multiple Group

Problems p.69-71

Fractions as Area Models Resource guide for using this book with unit concepts (4.NE.3, 4.NE.4)

**Gather and** study the **RESOURCES** 











### Options for Assessment – available online for Unit 3

### **Essential Question 1**

How do I use comparisons to reason about size and quantity? (specifically 4.OA.1 and 4.OA.2)

PARCC	Illustrative Mathematics	
Partnership for Assessment of Bradiness for College and Careers	4.OA Comparing Money Raised	d
	Alignments to Content Standa	rds
Ms. Morales has a bag of beads.	Alignment: 4.0A.A.2 Tags	
<ul> <li>She gives Elena 5 beads.</li> <li>She gives Damian 8 more beads than Elena.</li> <li>She gives Trish 4 times as many beads as Damian.</li> </ul>	• This task is not yet tagged.	
Ms. Morales then has 10 beads left in the bag.	a. Helen raised \$12 for the food bank las much money did she raise this year?	t year and she raised 6 times as much money this year. How
	b. Sandra raised \$15 for the PTA and Ni compared to Sandra?	Illustrative Mathematics
Part A	c. Luis raised \$45 for the animal shelter, much money did Anthony raise?	4.NBT.1 Threatened and Endangered
How many beads did Damian and Trish each receive? Show or explain how you arrived at each answer.		Alignments to Content Standards <ul> <li>Alignment: 4.NBT.A.1</li> </ul>
Cet Paste Undo Redo	_	Alignment: 4.0A.A.1 Tags
		This task is not yet tagged.
		Maned wolves are a threatened species that live in South America. People estimate that there are about 24,000 of them living in the wild.
Part B How many beads were in Ms. Morales' bag before any beads were given to students?		
		10

Esse	ntial Questions	5
Hanti an CARTY as TRADUCES Mice and as SCOUCE DISCUSSION In Mice and Association In Mice and Associati	Nata ur inner Sandanist Market Alssinder Alssinderviji Mer Alssinderviji	Daay LESSONS TECHNOLOU

Make or locate SUMMATIVE and PERFORMANCE ASSESSMENTS

#### Backward Unit Planning 1.0 Options for Assessment – available online for Unit 3 **Essential Questions Essential Question 1** How do I use comparisons to reason Make or locate about size and quantity? **SUMMATIVE** (specifically 4.MD.1 and 4.MD.2) and PERFORMANCE **ASSESSMENTS** Θ Review 🎮 Flag GRADE 4 MATHEMATICS / SESSION 1 / 5 OF 36 Illustrative Mathematics The length of a desktop is 4 feet. How many inches is the length of the desktop? 4.MD Who is the tallest? Enter your answer in the box. Alignments to Content Standards Alignment: 4.MD.A.1 inches Tags This task is not yet tagged. Partnership for Assessment of Readiness for College and Careers Mr. Liu asked the students in his fourth grade class to measure their heights. Here are some of the heights they recorded: Student Height 50 inches Sarah 4 1/4 feet Jake 1 1 yards Andy 4 feet and 4 Emily inches List the four students from tallest to shortest.

### Options for Assessment – available online for Unit 3

### **Essential Question 2**

How can I use what I know about whole numbers to help me understand fraction operations?





hundredths

d. 5 hundredths + 2 tenths =

Backward Unit Planning 1.0

# LESSONS AND RESOURCES ARE AVAILABLE ONLINE.





# **NEW Teacher Created Resources pages!!!**





Beth Pesnell Elementary Curriculum Specialist bpesnell@rps.k12.ar.us

