

**MATHEMATICAL IDEAS & CONCEPTS:**

- Continue to represent and solve problems involving multiplication and division
- Continue to solve two-step word problems involving addition and subtraction
- Continue to add and subtract within 1000
- Understand place value *new this quarter*
- Continue to develop understanding of fractions
- Solve problems involving time *new this quarter*
- Reason with shapes and their attributes *new this quarter*
- Represent and interpret data *new this quarter*

ESSENTIAL QUESTIONS:

1. How are multiplication and division related?
2. How can I use notation to represent my strategies for addition and subtraction?
3. How can I build four-digit numbers in more than one way?
4. How can a fraction be represented in a variety of ways?
5. How can shapes belong to multiple categories?

STANDARDS:

Aligned to Essential Questions; Big Idea/Concept Standard (★) with supporting standards (→) connected below

Notes in gray font are from the AR Mathematics standards; RPS instructional pacing notes are in red font

- ★ **3.OA.D.8** Solve two-step word problems using the four operations, and be able to:
 - Represent these problems using *equations* with a letter standing for unknown quantity
 - Assess the reasonableness of answers using mental computation and estimation strategies including rounding

Q2 Focus: addition/subtraction; multiplication/division involving facts of 2, 5, and 10

Note: 3.OA.D.8 This standard is limited to problems posed with whole numbers and having whole-number answers; students should know how to perform operations in conventional order when there are no parentheses to specify a particular order (Order of Operations).

***This standard is not listed with a specific essential question because it should be embedded throughout all aspects of their mathematical work this year.*

EQ 1: How are multiplication and division related?

- ★ **3.OA.A.3** Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities (e.g., by using drawings and *equations* with a symbol for the unknown number to represent the problem)
 - **3.OA.A.1** Interpret *products* of *whole numbers* (e.g., interpret 5×7 as the total number of objects in 5 groups of 7 objects each)
For example: Describe a context in which a total number of objects can be expressed as 5×7 .
 - **3.OA.A.2** Interpret whole-number *quotients* of *whole numbers* (e.g., interpret $56 \div 8$ as the number of objects in each share when 56 objects are partitioned equally into 8 shares, or as a number of shares when 56 objects are partitioned into equal shares of 8 objects each)
For example: Describe a context in which a number of shares or a number of groups can be expressed as $56 \div 8$
 - **3.OA.A.4** Determine the unknown whole number in a multiplication or division equation relating three *whole numbers* *new this quarter*
For example: Determine the unknown number that makes the equation true in each of the *equations* $8 \times ? = 48$; $5 = _ \div 3$; $6 \times 6 = ?$
 - **3.OA.B.6** Understand division as an unknown-factor problem. *new this quarter*
For example: Find $32 \div 8$ by finding the number that makes 32 when multiplied by 8

Standards associated with this essential standard continue on next page...



EQ 1: How are multiplication and division related? continued...

★ **3.OA.C.7** *Q2 Expectation: Fluency with 0, 1, 3, and 4 facts; Maintain fluency with 2, 10, 5 facts*

- Using *computational fluency*, multiply and divide within 100, using strategies such as the relationship between multiplication and division (e.g., knowing that $8 \times 5 = 40$, one knows $40 \div 5 = 8$) or properties of operations
- By the end of Grade 3, automatically (*fact fluency*) recall all *products* of two one-digit numbers

Note: 3.OA.C.7 Computational fluency is defined as a student's ability to efficiently and accurately solve a problem with some degree of flexibility with their strategies

→ **3.OA.B.5** Apply properties of operations as strategies to multiply and divide. *Note: 3.OA.B.5 Students are not required to use formal terms for these properties.*

For example:

- If $6 \times 4 = 24$ is known, then $4 \times 6 = 24$ is also known (*Commutative property of multiplication*).
- $3 \times 5 \times 2$ can be found by $3 \times 5 = 15$, then $15 \times 2 = 30$, or by $5 \times 2 = 10$, then $3 \times 10 = 30$ (*Associative property of multiplication*).
- Knowing that $8 \times 5 = 40$ and $8 \times 2 = 16$, one can find 8×7 as $8 \times (5 + 2) = (8 \times 5) + (8 \times 2) = 40 + 16 = 56$ (*Distributive property*)

EQ 2: How can I use notation to represent my strategies for addition and subtraction?

★ **3.NBT.A.2** Using *computational fluency*, add and subtract within 1000 using strategies and *algorithms* based on *place value*, properties of operations, and the relationship between addition and subtraction.

Note: 3.NBT.A.2 Computational fluency is defined as a student's ability to efficiently and accurately solve a problem with some degree of flexibility with their strategies.

→ **3.NBT.A.1** Use *place value* understanding to round *whole numbers* to the nearest 10 or 100.

EQ 3: How can I build four-digit numbers in more than one way?

★ **3.NBT.A.4** Understand that the four digits of a four-digit number represent amounts of thousands, hundreds, tens, and ones (e.g., 7,706 can be portrayed in a variety of ways according to *place value* strategies). *new this quarter*

Understand the following as special cases:

- 1,000 can be thought of as a group of ten hundreds---called a thousand
- The numbers 1,000, 2,000, 3,000, 4,000, 5,000, 6,000, 7,000, 8,000, 9,000 refer to one, two, three, four, five, six, seven, eight, or nine thousands

→ **3.NBT.A.5** Read and write numbers to 10,000 using base-ten numerals, number names, and *expanded form(s)*. *new this quarter*

For example:

- Using base-ten numerals "standard form" (347)
- Number name form (three-hundred forty seven)
- *Expanded form(s)* ($300 + 40 + 7 = 3 \times 100 + 4 \times 10 + 7 \times 1$)

Q2 Focus: multiple experiences using models and manipulatives to build four-digit numbers in a variety of ways



EQ 4: How can a fraction be represented in a variety of ways?

Note: Grade 3 expectations in this domain are limited to fractions with denominators 2, 3, 4, 6, and 8

★ 3.NF.A.1

- Understand a *fraction* $1/b$ as the quantity formed by 1 part when a whole is partitioned into b equal parts. For example: Unit fractions are fractions with a numerator of 1 derived from a whole partitioned into equal parts and having 1 of those equal parts ($\frac{1}{4}$ is 1 part of 4 equal parts).
- Understand a *fraction* a/b as the quantity formed by a parts of size $1/b$. For example: Unit fractions can be joined together to make non-unit fractions ($\frac{1}{4} + \frac{1}{4} + \frac{1}{4} = \frac{3}{4}$).

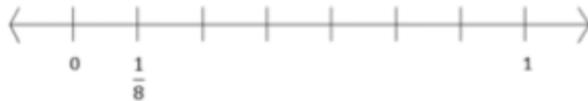
→ 3.G.A.2

- Partition shapes into parts with equal areas
- Express the area of each part as a *unit fraction* of the whole. For example: Partition a shape into 4 parts with equal area, and describe the area of each part as $1/4$ of the area of the shape.

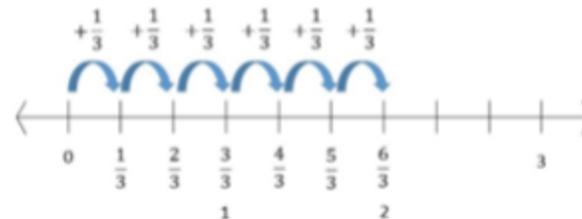
★ 3.NF.A.2 Understand a *fraction* as a number on the number line; represent *fractions* on a *number line diagram*: *new this quarter*

- Represent a *fraction* $1/b$ on a *number line diagram* by defining the interval from 0 to 1 as the whole and partitioning it into b equal parts
- Recognize that each part has size $1/b$ and that the endpoint of the part based at 0 locates the number $1/b$ on the number line (see example 1)
- Represent a *fraction* a/b on a *number line diagram* by marking off a lengths $1/b$ from 0
- Recognize that the resulting interval has size a/b and that its endpoint locates the number a/b on the number line (see example 2)

Example 1



Example 2



★ 3.NF.A.3 Explain equivalence of *fractions* in special cases and compare *fractions* by reasoning about their size: *new this quarter; formally assessed in Q3/Q4*

- Understand two *fractions* as equivalent (equal) if they are the same size or the same point on a number line
- Recognize and generate simple equivalent *fractions* (e.g., $1/2 = 2/4$, $4/6 = 2/3$)
- Explain why the *fractions* are equivalent (e.g., by using a *visual fraction model*)
- Express *whole numbers* as *fractions* and recognize *fractions* that are equivalent to *whole numbers* (e.g., Express 3 in the form $3 = 3/1$; recognize that $6/1 = 6$; locate $4/4$ and 1 at the same point of a *number line diagram*)
- Compare two *fractions* with the same *numerator* or the same *denominator* by reasoning about their size. Recognize that comparisons are valid only when the two *fractions* refer to the same whole. Record the results of comparisons with symbols ($>$, $=$, $<$) and justify the conclusions (e.g., by using a *visual fraction model*)



EQ 5: How can shapes belong to multiple categories?

★ **3.G.A.1** *new this quarter*

- Understand that shapes in different categories (e.g., rhombuses, rectangles, and others) may share *attributes* (e.g., having four sides) and that the shared *attributes* can define a larger category (e.g., quadrilaterals)
- Recognize rhombuses, rectangles, and squares as examples of quadrilaterals, and draw examples of quadrilaterals that do not belong to any of these subcategories

Additional Standards:

→ **3.MD.A.1** *Q2 Focus: measuring time intervals and solving problems involving elapsed time*

- Tell time using the terms quarter and half as related to the hour (e.g., quarter-past 3:00, half-past 4:00, and quarter till 3:00)
Connect to fractional understandings (NF.A.1, NF.A.2)
- Tell and write time to the nearest minute and measure time intervals in minutes
- Solve word problems involving addition and subtraction of time intervals in minutes (e.g., by representing the problem on a *number line diagram*)

→ **3.MD.B.3** *new this quarter*

- Draw a scaled picture graph and a scaled bar graph to represent a data set with several categories (e.g., Draw a bar graph in which each square in the bar graph might represent 5 pets)
- Solve one- and two-step "how many more" and "how many less" problems using information presented in scaled picture graphs and scaled bar graphs